Data and the Aggregate Economy

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2019 Meeting of Society for Economic Dynamics
Data in the Aggregate Economy

- Data can be encoded as binary sequence of zeroes and ones.
  - This includes music, poetry, patents ... not my focus
  - My focus: statistics and records of transactions.

- Entering a new era: Big data is the industrialization of knowledge production
  - Replaces artisanal production and mitigates diminishing returns to data.

- When we transitioned from agrarian to industrial, we replaced land with capital in production functions.
  As we transition again, what if production includes data?
1. **Data is changing every corner of macroeconomics**
   - A quick tour through many facts/questions.

2. **Existing theoretical tools to understand data**
   - How data is similar to and different from technology?
   - Relevant tools from information frictions literature

3. **Framework to explore effect of data on aggregate economic activity**
GDP Measurement

- Measured data GDP is large and growing: information and communications tech (ICT) ≡ 6.5% of global GDP, \( \sim \) 100 million workers (UN (2017))

- Most data is not in GDP because it’s bartered.
  - Consumers give data in exchange for a service.
  - Not priced → Not captured by GDP

- Big question: Might it explain productivity slowdown?
  - Yes: Brynjolfsson et al. (2017)
  - No, effect too small: Syverson (2017)
Will the data economy negate geography?

“... [W]e are determined to take full advantage of the digital revolution. This revolution is summed up by the fact that it no longer is of utmost importance where you are but rather what you can do ...”

— Rwandan President Paul Kagame (2010)

Data reduces language barriers

- Machine translation increases exports by 17.5% through reduction in search costs (Brynjolfsson et al. (2018))

Control of data is a significant issue in trade negotiations.
Are we exporting data assets at zero price to foreign entities?
Digital economy changes how firms adjust prices.

Price changes occur more frequently in online stores than in regular stores (Gorodichenko and Talavera (2017))

- Every 3 weeks or less for online stores
- Every 4-5 months or more for regular stores

Might more price flexibility reduce monetary policy effectiveness?
Will artificial intelligence displace labor?
AI ↓es labor, but ↑ labor productivity in non-automated tasks
(Acemoglu and Restrepo (2018))

Will data reduce search frictions?
IT investment boosts firms’ efficiency (Aral and Weill (2007)), especially large firms
(Tambe and Hitt (2012), Brynjolfsson and McElheran (2016))

Data also affects firm size through finance
  - Big data in financial markets can lower the cost of capital for large firms (Begenau, Farboodi, Veldkamp (2018))

Market power? Data could be a barrier to entry.
AND AFTER BIG DATA SOLVES ALL OUR PROBLEMS, WE'LL RIDE AWAY ON MAGIC FLYING UNICORNS.

Tools to think sensibly about data
Data enhances productivity, is non-rival, has returns to scale. 
(Jones and Tonetti (2018), Agrawal et al. (2018), Lu (2019), Aghion et al. (2017)) 
Current thinking: This makes data just like ideas.

Data can be traded like ideas/patents, but a little different:
- Can be described without revealing information content.
- While technologies leak (Easterly (2002)), data is not embodied in human capital. Less likely to diffuse.
Ideas From Information Frictions: Where does data come from?

- Data is a by-product of economic activity
  - had aggregate productivity data.
  - I’ll adapt these to make data good-specific.
- Unlike tech, incentives/rents not required to produce.

- Costly information acquisition and information markets

- Talking about data overcomes 3 barriers to information literature:
  1. We can’t measure information. Bytes are countable.
  2. We can’t integrated it into standard recursive dynamic models.
  3. What important macro question can’t be answered without it?
Why model data?
- Macroeconomists should have something to say about the information economy. It’s an aggregate phenomenon.
- Answer policy questions: regulation, tariffs.
- Learn how to value data.

What features does a macro-data theory need?
- Data is a by-product of economic activity.
- Firms with data make better forecasts, are more productive.
- Data is a valuable asset.
Main results

1. Data has diminishing returns, cannot sustain growth without technological progress.

2. Cross-firm inequality rises, then falls.

3. Some firms specialize in data production.

4. Optimal goods price can be zero (data barter).
A Model of Data as a Productive Asset
A continuum of competitive firms $i$

Each firm produces $k_{i,t}^\alpha$ units of goods with $k_{i,t}$ units of capital

These goods have quality $A_{i,t}$

Firms take equilibrium price $P_t$ as given and their quality-adjusted outputs are perfect substitutes

$$P_t = \bar{P} Y_t^{-\gamma},$$

$$Y_t = \int_i A_{i,t} k_{i,t}^\alpha di$$
Model: How Data Improves Goods Quality

- Quality depends on chosen production technique \(a_{i,t}\)
- Firm has one optimal technique: \(\theta_{i,t} + \varepsilon_{a,i,t}\)
  - \(\theta_{i,t}\) is an AR(1), with innovation \(\eta_{i,t} \sim N(\mu, \sigma^2_\theta)\).
  - \(\varepsilon_{a,i,t} \sim N(0, \sigma^2_a)\) is unlearnable and i.i.d.

\[
A_{i,t} = \hat{A} - (a_{i,t} - (\theta_{i,t} + \varepsilon_{a,i,t}))^2
\]

- Data is a by-product of \(t - 1\) production: \(n_{i,t} = z_i k_{i,t-1}\)
- \(z\) is data-mining ability.

- Each data point \(m \in [1 : n_{i,t}]\) reveals
  \(s_{i,t,m} = \theta_{i,t} + \epsilon_{i,t,m}\) where \(\epsilon_{i,t,m} \sim N(0, \sigma^2_\epsilon)\).
- Data adjustment cost: \(\Psi(\cdot)\).
A Simple Recursive Solution

- **State variable: Stock of knowledge**

\[
\Omega_{i,t} \equiv \mathbb{E}\left[ (\mathbb{E}[\theta_i,t|\mathcal{I}_{i,t}] - \theta_i,t)^2 |\mathcal{I}_{i,t} \right]^{-1}
\]

(Posterior precision)

\[
\mathbb{E}[A_{i,t}] = \hat{A} - \Omega_{i,t}^{-1} - \sigma_a^2
\]

(Expected quality)

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The optimal sequence of capital investment choices \( \{k_{i,t}\} \) solves the recursive problem:

\[
V(\Omega_{i,t}) = \max_{\{k_{i,t}\}} P_t (\hat{A} - \Omega_{i,t}^{-1} - \sigma_a^2) k_{i,t}^\alpha - P_t \Psi(\Delta \Omega_{i,t+1}) - r k_{i,t} + \beta V(\Omega_{i,t+1})
\]

where \( n_{i,t+1} = z_i k_{i,t}^\alpha \) and (Kalman filter)

\[
\Omega_{i,t+1} = \left[ \rho^2 (\Omega_{i,t} + \sigma_a^{-2})^{-1} + \sigma_\theta^2 \right]^{-1} + n_{i,t+1} \sigma_\epsilon^{-2}
\]
Firm’s stock of knowledge, $\Omega_{i,t}$, is a discounted sum of data "investments."

$$\frac{\partial V_t}{\partial \Omega_{i,t}} = \text{Marginal value of one additional piece of data (additional unit of precision).}$$

$$= \text{price of data}$$

The optimal price of goods may be zero (data barter)

To generate transactions and accumulate data:

$$V'(\Omega_{t+1}) > 0.$$
Data Growth, Solow-Style

- Inflows: \( z_i k_{it}^\alpha \sigma^{-2} \) (# of data points \( \times \) precision)
- Outflows: data depreciation
- Steady state: inflows = outflows

Concavity: Infinite data \( \rightarrow \) perfect foresight \( \rightarrow \) finite productivity.
**Takeaway:** Data has increasing, then diminishing returns (Bajari et al. (2018)).

Data $\rightarrow$ more output $\rightarrow$ more data, until forecast error $\rightarrow$ 0.
How Firms’ Data Stock Grows Over Time

- Three firms with different initial data stocks.

Data convergence, with different initial data stocks

Divergence, then convergence. Inequality is transitory?
Inflows and outflows the same. $P_t$ now adjusts.

Eqbm $\rightarrow$ Faster early growth bc initial goods price is high.
Use precision $\omega$ at price $\pi$:
$\omega < (>) n$ is selling (buying) data.

$$V(\Omega_{i,t}) = \max_{\{k_{i,t}, \omega_{it}\}} P_t(\bar{A} - \Omega_{i,t}^{-1} - \sigma_a^2) k_{i,t}^\alpha + \pi(n_{i,t+1} - \omega_{it})$$

$$- \Psi(\Delta\Omega_{i,t+1}) - rk_{i,t} + \beta V(\Omega_{i,t+1})$$

$$\Omega_{i,t+1} = \left[\rho^2(\Omega_{i,t} + \sigma_a^{-2})^{-1} + \sigma_\theta^2\right]^{-1} + \omega_{it}$$

Without adjustment frictions ($\Psi = 0$), immediate convergence.
Tradeable Data:
Unproductive data miner \((z_i = 1)\) sells then buys data

![Graph]

Early data sales avoid data adjustment cost. Firm doesn’t have systems in place to use their own data.
Tradeable Data:
Data miners \((z_i = 15)\) sell most of their data.

Data miners don’t use much data. They don’t need high-quality goods. Most revenue from data sales.
Lots of data used for advertising. Maybe not socially productive. Does this overturn results?

Suppose data processing helps the firm that uses it, but has no social value:
(Morris-Shin (2002))

\[ A_{i,t} = \hat{A} - (a_{i,t} - \theta_{i,t} - \epsilon_{a,i,t})^2 + \int_{j=0}^{1} (a_{j,t} - \theta_{j,t} - \epsilon_{a,j,t})^2 \, dj \]

Result: Same results as figures above. Logic holds for either case. This doesn’t change firms’ choices or firm dynamics. Does affect aggregate quality and welfare.
Many ways to enrich this model

- **Non-rival data requires imperfect competition.**
  (See Jones-Tonetti, 2019.)

- **Data market where high-demand data has lower price** (Veldkamp 2006) or data provider chooses what to provide (Nimark, 2014)
  $\rightarrow$ Realistic business cycle variance and covariance.

- Choice of what data to purchase / process:
  Rational inattention tools originally developed for data allocation. Stylized version of AI.
  - Sims (2003), Mackowiak-Wiederholt (2009), Woodford(2009), Matejka-McKay(2015), Kacperczyk-VNV (2016)... 

- **Firm entry / exit**

- **Agents use data to learn about the distribution of shocks**
  (Kozlowski-Veldkamp- Venkateswaran, 2019)
  $\rightarrow$ persistent responses to unusual events.
Conclusions

- Data is an important asset in the modern economy ... like capital.

- Has some features of tech: non-rival, raises productivity.
  - Key difference: As forecast errors get smaller, most information has decreasing returns.

- Data may be changing the allocation of rents in the economy ... but not its fundamental economics.

- Open questions for theory and data:
  - How much of the superstar firm phenomenon is due to data economics?
  - Has data changed the returns to capital / labor?
  - How do we value firms whose main asset is data?
  - ... and many more
"Big" data is so sad. With me, you will get "yuge" data, and we will make data great again!
Questions & Comments