Channel, Deadline, and Distortion ($CD^2$) Aware Scheduling for Video Streams Over Wireless

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Abstract

We study scheduling of multimedia traffic on the downlink of a wireless communication system. We examine a scenario where multimedia packets are associated with strict deadlines and are equivalent to lost packets if they arrive after their associated deadlines. Lost packets result in degradation of playout quality at the receiver, which is quantified in terms of the “distortion cost” associated with each packet. Our goal is to design a scheduler which minimizes the aggregate distortion cost over all receivers. We study the scheduling problem in a dynamic programming (DP) framework. Under well justified modeling reductions, we extensively characterize structural properties of the optimal control associated with the DP problem. We leverage these properties to design a low-complexity Channel, Deadline, and Distortion ($CD^2$) aware heuristic scheduling policy amenable to implementation in real wireless systems. We evaluate the performance of $CD^2$ via trace-driven simulations using H.264/MPEG-4 AVC coded video. Our experimental results show that $CD^2$ comfortably outperforms benchmark schedulers like earliest deadline first (EDF) and best channel first (BCF). $CD^2$ achieves these performance gains by using the knowledge of packet deadlines, wireless channel conditions, and application specific information (per-packet distortion costs) in a systematic and unified way for multimedia scheduling.

Index Terms

Wireless networks, video streaming, packet scheduling, dynamic programming.

I. INTRODUCTION

The advent of the third generation (3G) of cellular wireless communication systems has sparked an ever increasing interest in mobile wireless multimedia applications like video streaming. Transmission of multimedia traffic over wireless links poses challenging theoretical as well as practical problems. This is attributed to temporal and spatial variations in wireless channel quality, stringent availability of resources like bandwidth, and unique characteristics of multimedia traffic such as packet interdependencies and deadline constraints.
Scheduling algorithms employed at the base station (BS) or access point (AP) play a key role in determining the performance of wireless systems. The problem of downlink scheduling, wherein a single transmitter at the BS is shared amongst multiple downlink users, has been studied extensively (see [1] for an overview). Most initial work in downlink scheduling focused on maximizing throughput and optimizing system performance for non-real-time delay tolerant traffic. The unifying thread for all this work was the idea of opportunistic scheduling (see [2] and references therein), which entails exploiting multiuser diversity inherent in wireless systems due to fluctuating channel conditions. However, such schedulers, being oblivious to packet deadlines, perform poorly in the context of delay-sensitive multimedia applications.

A. Related work

More recently, the idea of deadline-aware packet scheduling has received attention in the wireless community. Georgiadis et. al. [3] showed the optimality of the earliest deadline first (EDF) scheduling policy for deadline constrained scheduling over wired (error-free) channels. However, EDF is not well-suited to the wireless scenario, owing to its disregard for channel variations. In [4], Shakkottai and Srikant modeled the wireless channel as a two-state ON-OFF Markov chain, and showed that using EDF for ON users in each time-slot is “nearly optimal” for minimizing the number of packets dropped due to missed deadlines. They were the first to study a channel-aware version of EDF. Khattab and Elsayed [5] proposed a heuristic channel dependent EDF policy, and demonstrated its performance gains via simulations.

In [6], Ren et. al. used dynamic programming (DP) for a simulation based study of scheduling constant bit-rate (CBR) traffic over wireless channels modeled as finite-state Markov chains. Johnsson and Cox [7] proposed a heuristic cost function, and showed via simulations that a policy which minimizes this cost function performs well with respect to the number of missed packet deadlines. Dua and Bambos [8] studied deadline and channel aware scheduling in a DP framework. They leveraged provable structural properties of the optimal solution to the DP problem to design low-complexity, near-optimal scheduling policies. Our current work is similar to [8] in spirit.

Even though schedulers proposed in the work cited above account for both channel conditions and packet deadlines, none of them take into consideration the unique characteristics of mul-
timedia traffic. Amongst the several authors who have explicitly accounted for characteristics of multimedia traffic, Chou and Miao [9] studied Rate-Distortion (RD) optimized streaming of packetized media. In their work, the “importance” of every packet is determined by its associated distortion value, and packet (re)-transmissions are scheduled in order to minimize distortion, given the rate constraint of the channel. Wee et. al. [10] focused on networks with large delay variations, and achieved improvements in video playout quality by maximizing the probability of on-time delivery of more important packets. Liebl et. al. [11] proposed a heuristic cost function which incorporates deadline, channel, and distortion information. They demonstrated via simulations that a scheduler which minimizes this cost yields considerable performance gains over benchmark schedulers. Apostolopoulos [12] examined low-complexity RD optimized streaming of multiple encrypted video streams over a shared bandwidth bottleneck. Chakareski and Frossard [13] studied RD optimized streaming of multiple video streams by prioritizing re-transmissions based on packet contents. They expressed their optimization problem in a Lagrangian framework and used sub-gradient methods to solve it. Kalman et. al. [14] used an expected peak signal-to-noise ratio (PSNR) maximization technique to examine scheduling of multiple transcoded video streams over a shared wireless link.

B. Our contributions and paper outline

Our goal in this work is to design a scheduling policy which combines knowledge of multimedia characteristics with deadline and wireless channel information in a systematic way to enhance system performance. We consider video transmission over wireless channels with time-varying reliability. Distortion is incurred at the receiver if a packet misses its playout deadline. Only one user can be scheduled in each time-slot. The scheduler must decide which user to schedule and which packet to transmit to the scheduled user in every time-slot to minimize aggregate distortion incurred over all users.

We present our system model in Section II, where we discuss the wireless channel model, the distortion cost model, and the optimal packet prioritization policy. In Section III, we formulate the scheduling problem as a dynamic programming (DP) problem [15], under well justified modeling assumptions. We then propose our Channel, Deadline, and Distortion (CD²) aware scheduling algorithm, based on a quasi-static approach to scheduling. CD² has the solution to
the DP problem at its core. In Section IV, we establish key structural properties of the optimal control for the DP problem. Prominent amongst these are the optimality of a switch-over policy [16], and the time-invariance of switch-over curves for a two-user system. Next, we show that the DP problem for a system with more than two users can be solved using a pairwise comparison approach. This leads to an implementation of $CD^2$ whose complexity grows only linearly with the number of users in the system. In Section V, we employ trace-driven simulations (using H.264/MPEG-4 AVC coded video) to demonstrate the efficacy of $CD^2$ and its performance gains (2-12dB increase in average PSNR) relative to benchmark schedulers like “earliest deadline first” and “best channel first”. We provide concluding remarks in Section VI.

II. Model Construction

We study a time-slotted wireless system with $N$ downlink users and a time-multiplexed scheduler $S$ at the BS. There is a queue corresponding to each downlink user at the BS, which buffers video frames the user wishes to receive. The queue for the $i^{th}$ user is denoted $Q_i$. A schematic of the system is depicted in Fig. 1. Each video frame is divided into multiple network packets. The video is encoded to achieve a roughly constant quality (measured in terms of PSNR) for each frame, which leads to a variable number of network packets per frame, depending on the difficulty in compressing each frame.

In each time-slot, $S$ schedules one packet from the head-of-line (HOL) frame of one of the $N$ queues for transmission according to some scheduling policy. The HOL frame of $Q_i$ consists of $n_i$ packets and is associated with a deadline $D_i$. This deadline reflects the time by which the frame must be received at the downlink receiver to ensure uninterrupted playout. All packets in the HOL frame share this common deadline. Any packets in the frame which are not successfully transmitted before the expiration of the deadline are dropped. This results in a degradation of video quality at the receiver due to increased distortion. The objective of the scheduler is to minimize aggregate distortion at the downlink receivers due to missed packet deadlines.

A. Wireless Channel Model

Wireless channels exhibit temporal and spatial fluctuations, which are attributed to user mobility, interference from concurrent transmissions, and signal attenuation due to physical phe-
nomena. Different models have been used in the literature to abstract this behavior of wireless channels. While some authors model the wireless channel as a reliable “bit-pipe” with time-varying capacity, others model it as a fixed-size “bit-pipe” with time-varying reliability. We adopt the latter approach and quantify the channel quality in time-slot $t$ by the probability of successful transmission of a packet over the channel, if the channel is used in time-slot $t$. For $Q_i$, we denote this success probability by $s^i_t$. For example, $s^i_t$ can be modeled as being modulated by an underlying finite-state Markov chain (FSMC) [17], where each state corresponds to a different probability of successful transmission. We employ a two-state FSMC model for performance evaluation in Section V. We further assume that the wireless channels from the BS to the downlink users are independent of each other.

**B. Distortion Costs**

If one or more packets in a frame miss their deadline, the decoder is forced to use error concealment techniques such as “previous frame copy”, and a distortion cost is incurred. We measure distortion in the mean-squared error (MSE) sense. The distortion cost associated with each packet, which expresses the packet’s application layer importance, is placed in the packet header and thereby is accessible to the scheduler [12].

We denote by $\omega_i(k_i)$ the distortion cost incurred if $k_i$ packets from the HOL frame of $Q_i$ miss their deadline. We assume that $\omega_i(k_i)$ is a non-negative, strictly increasing, and convex function of $k_i \forall i$. While the first two assumptions are consistent with intuition, the convexity assumption is corroborated by empirical data. Fig. 2 depicts plots of $\omega_i(k_i)$ for four different frames of the “Foreman sequence” (a test sequence widely used by the video community) in CIF format encoded using H.264/MPEG-4 AVC with a single leading I-frame followed by 349 P-frames. Observe that the empirical results are in accordance with our assumptions.

We compute $\omega_i(k_i)$ by dropping packets, decoding, and computing the resultant MSE. We assume that distortion is additive across multiple dropped packets. There are $2^K$ possible ways (dropping patterns) of dropping packets from a frame comprised of $K$ packets. $\omega_i(1)$ is defined as the minimum MSE distortion incurred by dropping only one packet from the HOL frame of $Q_i$. $\omega_i(k_i + 1)$ is defined as the minimum MSE distortion incurred by dropping one more packet, in addition to the packets dropped to incur $\omega_i(k_i)$. This embedded computation of $\omega_i(k_i)$ imposes
a rank ordering on the packets within a frame, which might be quite different from the ordering imposed by encoding. These computations are performed offline at the time of encoding, and the results are placed in the packet/frame headers, so that they are readily available to a distortion-aware scheduler. The rank of a packet in a frame expresses its priority for transmission by a distortion-aware scheduler. The number of dropping patterns now reduces to $K + 1$ from $2^K$.

III. Problem Formulation

In general, the scheduling problem can be formulated within a control/optimization framework and solved using numerical techniques, given statistical characterizations or actual realizations of the distortion cost curves and channel conditions for all users. Such an approach, apart from being computationally prohibitive from an implementation perspective, does not provide insight into the fundamental trade-offs inherent in the scheduling problem. Moreover, detailed knowledge of traffic or channel conditions is not available to the scheduler in real wireless systems. We seek a formulation which encapsulates the fundamental scheduling tradeoffs, is amenable to analysis, and leads to implementation friendly scheduling policies. To this end, we (sequentially) introduce two modeling reductions.

- **Modeling Reduction R1**: To formulate our optimal control problem, we assume that each queue contains only one frame.
- **Modeling Reduction R2**: We assume static (in a probabilistic sense) channel conditions in the control problem formulated under reduction R1.

The ultimate test to determine the validity of the reductions is the “test against nature”, that is, to test whether policies based on the properties of the solution to the reduced problem perform better than benchmark policies or not, in real-world scenarios. Our experimental results presented in Section V show that this is indeed the case for $CD^2$.

A. Single frame offline optimal — problem formulation under R1 only

We first study the optimal control problem which incorporates reduction R1 only. In Section III-B, we will study a control problem which incorporates both reductions.

R1 is a reasonable assumption if the frames are being generated periodically by a real-time media source, so that a new frame arrives to a queue only after the current frame has
been transmitted. This assumption is also consistent with the principles of low-latency media system design. We consider a finite time-horizon of $T$ time-slots starting at $t = 1$, where $T = \max(D_1, \ldots, D_N)$ and $D_i$ is the deadline associated with the HOL frame of $Q_i$. The deadlines on all HOL frames expires by the end of the time-horizon $T$. Any residual packets at the end of the horizon are dropped and a cost is incurred, as described in Section II-B.

Our objective is to design a scheduling policy which minimizes the sum, over all users, of expected dropping costs at the end of time-horizon $T$. The scheduler is assumed to know the channel statistics in terms of success probabilities for all users in time-slots $t = 1, \ldots, T$. We call this problem the single frame offline optimal and the associated optimal control policy $P^*(N)$.

We adopt the methodology of dynamic programming (DP) to compute $P^*(N)$. Let $n = (n_1, \ldots, n_N)$ denote the state of the system*, where $n_i$ is the number of remaining packets in the HOL frame of $Q_i$ at the beginning of the current time-slot. If $Q_i$ is scheduled in time-slot $t$, the state in time-slot $t + 1$ changes to $n - e_i$ with probability (w.p.) $s_i^t$ (transmission successful) and $n$ w.p. $\bar{s}_i^t \triangleq 1 - s_i^t$ (transmission fails). Here $e_i$ is the standard $i^{th}$ unit vector in $\mathbb{R}^N$, that is, $e_i = (0, \ldots, 0, 1, 0, \ldots, 0)$ with the 1 in the $i^{th}$ location. Without loss of generality, we assume $0 < D_1 \leq \ldots \leq D_N = T$. The assumption implies that $Q_i$ is not a scheduling candidate after $t = D_i < T$, since the deadline on its HOL frame expires in time-slot $t = D_i$.

Denote by $V^t(n)$ the expected cost-to-go in time-slot $t$, starting in state $n$. By definition, $V^t(n)$ is the minimum expected cost incurred by the optimal policy $P^*(N)$ over time-slots $t, \ldots, T$, starting in state $n$ in time-slot $t$. $V^t(n)$ is computed from the following recursive DP equations:

$$V^t(n) = \min_{i=1, \ldots, N} \left\{ \alpha_i^t(n) \right\} + V^{t+1}(n), \quad t = 1, \ldots, T,$$

and the boundary conditions $V^{T+1}(n) = \sum_{i=1}^{N} \omega_i(n_i)$, where

$$\alpha_i^t(n) = \begin{cases} s_i^t[V^{t+1}(n - e_i) - V^{t+1}(n)], & n_i > 0, t \leq D_i \\ 0, & \text{else}. \end{cases}$$

Setting $\alpha_i^t(n) = 0$ when $n_i = 0$ or $t > D_i$ eliminates $Q_i$ from consideration as a scheduling

*All vectors are denoted in **boldface**.
candidate when $Q_i$ is empty, or the deadline on its HOL frame has expired.

Solving the DP equations to compute $\mathcal{P}^*(N)$ requires non-causal knowledge of channel conditions over a period of $T$ time-slots, which is unavailable to the scheduler in real wireless systems. Thus, the single frame offline optimal (based on R1 alone) does not immediately lead to implementable scheduling policies.

**B. A quasi-static approach to scheduling — $CD^2$**

Motivated by the foregoing discussion, we now introduce reduction R2 into the our formulation, in addition to R1. Under R2, the probability of successful transmission is fixed for each user over a horizon of $T$ time-slots. Equivalently $s^t_i = s_i$ for $t = 1, \ldots, T, \forall i$. This is a reasonable assumption for slowly varying channels. We denote the optimal control in this case by $\mathcal{P}^*_s(N)$, which is computed via (1) and (2), with $s^t_i$ replaced by $s_i$. Thus, $\mathcal{P}^*_s(N)$ is a special case of $\mathcal{P}^*(N)$ where the success probability for each user is constant over the horizon $T$ of interest.

How does $\mathcal{P}^*_s(N)$ translate into an implementable scheduling policy? To answer this question, we propose a *quasi-static* approach to scheduling. We name our proposed policy $CD^2$, since it is a Channel, Deadline, and Distortion aware scheduling policy. The key steps in $CD^2$ are:

1) Given a system characterization in terms of instantaneous channel conditions, HOL frame deadlines, and number of packets in the HOL frame of each queue in the current time-slot, compute $\mathcal{P}^*_s(N)$ by solving (1) and (2) under the assumptions imposed by R1 and R2.

2) Schedule a packet in the system based on the decision of $\mathcal{P}^*_s(N)$ computed in Step 1.

3) Update the system parameters based on the outcome of Step 2 and most recently acquired channel knowledge (through receiver feedback or measurements made by the BS).

4) Repeat steps 1-3 in every time-slot.

Thus, the scheduling decision of $CD^2$ in each time-slot is based on the static channel assumption (R2). However, the static operating point is updated in each time-slot as wireless channels evolve over time. This justifies the nomenclature quasi-static. Note that $CD^2$ requires only instantaneous channel knowledge, rather than non-causal channel knowledge or a detailed statistical characterization of the channel behavior.

We reiterate that $CD^2$ is based on $\mathcal{P}^*_s(N)$, which is the optimal control policy for the scheduling problem formulated under modeling reductions R1 and R2. The gains provided by
CD² relative to benchmark policies (Section V) provide ample justification for our reductions, both from a modeling and an implementation perspective.

IV. STRUCTURAL PROPERTIES OF $P_s^*(N)$

In this section, we present important structural properties of $P_s^*(N)$, which is at the core of CD². We initially focus on a two-user scenario ($N = 2$), and show in Section IV-B that $P_s^*(N)$ for $N > 2$ can be computed by using $P_s^*(2)$ multiple times in a pairwise fashion.

A. Key properties of $P_s^*(2)$

To make the static channel assumption (R2) explicit, we suppress the superscript $t$ from the successful transmission probabilities and simply denote them by $s_1$ and $s_2$. Once again, we assume without any loss of generality that $D_1 < D_2$. Thus, $Q_1$ is a scheduling candidate for $t = 1, \ldots, D_1$ provided $n_1 > 0$, while $Q_2$ is a scheduling candidate over the entire time-horizon provided $n_2 > 0$. We employ the notation $n = (n_1, n_2)$, $e_1 = (1, 0)$, and $e_2 = (0, 1)$. Since no scheduling decision needs to be made after $t = D_1$ ($Q_2$ is scheduled, if non-empty), we reformulate our control problem for a time-horizon of length $T = D_1$ (instead of $D_2$, as in Section II). The DP equations can be re-written as

$$V^t(n) = \min \{\alpha_1^t(n), \alpha_2^t(n)\} + V^{t+1}(n), \quad t = 1, \ldots, T,$$

along with the boundary conditions $V^{T+1}(n) = \omega_1(n_1) + \phi_2(n_2, D_2 - D_1)$, where

$$\alpha_i^t(n) = \begin{cases} s_i[V^{t+1}(n - e_i) - V^{t+1}(n)], & n_i > 0 \\ 0, & \text{else} \end{cases},$$

and $\phi_2(\cdot, \cdot)$ is computed via the recursion

$$\phi_2(y, t) = \begin{cases} 0, & y = 0 \\ s_2\phi_2(y - 1, t - 1) + \bar{s}_2\phi_2(y, t - 1), & y, t > 0 \\ \omega_2(y), & t = 0. \end{cases}$$

Here, $\omega_1(n_1)$ is the distortion cost associated with dropping $n_1$ packets from $Q_1$ at the end of the time-horizon, while $\phi_2(n_2, D_2 - D_1)$ is the expected distortion cost incurred in transmitting $n_2$.
packets from $Q_2$ over a static channel with success probability $s_2$ during time-slots $T+1, \ldots, D_2$.

**Lemma 1:** \[ \phi_2(y,t) = \sum_{j=0}^{\min\{y,t\}} \binom{t}{j} \omega_2(y-j)s_2^j(1-s_2)^{t-j}. \]

**Lemma 2:** $\phi_2(y,t)$ is a non-increasing and convex function of $y$ for fixed $t$.

Now, define the decision function $\gamma^t(n)$ by

\[ \gamma^t(n) \triangleq \alpha^t_1(n) - \alpha^t_2(n), \quad t = 1, \ldots, T. \]  

Clearly, $P^*_s(2)$ schedules $Q_1$ in state $n$ in time-slot $t$ if $\gamma^t(n) \leq 0$, and schedules $Q_2$ else. Thus, $P^*_s(2)$ is completely determined by the sign of $\gamma^t(n)$. We now state a key property of $\gamma^t(n)$.

**Lemma 3:** $\gamma^t(n)$ is a non-increasing function of $n_1$ and a non-decreasing function of $n_2$.

An immediate and important consequence of Lemma 3 is the optimality of a switch-over type policy in each time-slot. We first formally define a switch-over type policy.

**Definition:** A scheduling policy is of switch-over type if in every time-slot $t$, the policy can be characterized by a non-decreasing switch-over curve $\psi^t : \mathbb{N} \mapsto \mathbb{N} \cup \{0\}$, such that the policy schedules $Q_2$ in time-slot $t$ if $n_2 > \psi^t(n_1)$, and schedules $Q_1$ else (see Fig. 3).

**Theorem 1 (Optimality of Switch-over Policy):** The policy $P^*_s(2)$ is of switch-over type.

The scheduling decision of $P^*_s(2)$ in the current time-slot ($t = 1$) is determined by $\psi^1$. Since our problem (3)-(5) is formulated as a backward recursion, one expects that $\psi^T, \ldots, \psi^2$ must be computed prior to computing $\psi^1$. Interestingly, our next result shows that this is not the case.

**Theorem 2 (Time-invariance):** The switch-over curves $\psi^t$ which characterize $P^*_s(2)$ are time-invariant, that is, $\psi^t = \psi, \forall \ t = 1, \ldots, T$.

Since the switch-over curves are time-invariant, computing the desired switch-over curve $\psi^1$ is equivalent to computing $\psi^T$. However, $\psi^T$ is determined by the sign of $\gamma^T(n)$, which was computed as a function of $\omega_1(\cdot)$ and $\phi_2(\cdot)$ in the proof of Lemma 3 (see Section VII-C). We reproduce the expression here for convenience:

\[ \gamma^T(n) = -s_1[\omega_1(n_1) - \omega_1(n_1-1)] + s_2[\phi_2(n_2, D_2 - D_1) - \phi_2(n_2-1, D_2 - D_1)]. \]

\[ \text{Proofs of all structural/theoretical results are available in the Appendix.} \]
Also, recall that $\phi_2(\cdot, \cdot)$ was computed as a function of $\omega_2(\cdot)$ in Lemma 1. In summary, $\psi^T$, and hence $\psi^1$ can be explicitly computed in terms of the distortion cost functions $\omega_1(\cdot)$ and $\omega_2(\cdot)$, which are available to the scheduler from the packet headers. The implication is that we have the optimal two-user policy for the scheduling problem formulated under reductions R1 and R2 in closed form. Note that the foregoing analysis is valid under the assumption $D_2 > D_1$. Analogous results for the case $D_1 > D_2$ are gotten by interchanging the roles of $Q_1$ and $Q_2$.

**B. Optimality of pairwise comparisons, and CD$^2$ re-visited**

How do the above results generalize to $P^*_s(N)$, the optimal control for a system with $N > 2$ users? To answer this question, we define the *pairwise decision functions*:

$$
\gamma_{ij}^t(n) \triangleq \alpha_i^t(n) - \alpha_j^t(n), \quad t = 1, \ldots, T.
$$

$P^*_s(N)$ “prefers” $Q_i$ over $Q_j$ in time-slot $t$ in state $n$ if $\gamma_{ij}^t(n) \leq 0$, and prefers $Q_j$ else. Now consider another decision rule, namely $\Pi_{PW}(N)(N)$, which discriminates between $Q_i$ and $Q_j$ in time-slot $t$ in state $n$ based on the sign of $\gamma_{ij}^t(n^{ij})$ instead of the sign of $\gamma_{ij}^t(n)$, where $n^{ij}$ agrees with $n$ in the $i^{th}$ and $j^{th}$ locations, and is zero elsewhere. $\Pi_{PW}(N)$ is therefore a *pairwise comparison* rule which solves the $N$-user problem as a sequence of two-user problems. Clearly, $P^*_s(N) = \Pi_{PW}(N)$ for $N = 2$. Does $P^*_s(N) = \Pi_{PW}(N) \forall N$? Yes!

**Theorem 3:** For the scheduling problem formulated under reductions R1 and R2, the pairwise comparison rule $\Pi_{PW}(N)$ is optimal, that is, $P^*_s(N) = \Pi_{PW}(N)$.

**Pairwise CD$^2$:** Recall from Section III-B that CD$^2$ computes $P^*_s(N)$ in each time-slot (Step 1) and schedules a packet in the system based on the decision of $P^*_s(N)$ (Step 2). Theorem 3 provides an alternative way of implementing Step 2 of CD$^2$, based on computing $P^*_s(N)$ by using the pairwise comparison rule $\Pi_{PW}(N)$. In Step 2 of pairwise CD$^2$, users are grouped randomly into pairs. Users within a pair are compared using policy $P^*_s(2)$, which is computable in closed form, as shown in Section IV-A. The winner of each pair is promoted to the next round. The process continues till only one user survives. This user is scheduled in the current time-slot. Implementation details of Step 2 of pairwise CD$^2$ are enumerated in Table I. Steps 1, 3, and 4 are identical to CD$^2$. 
Pairwise $CD^2$ based on $\Pi_{pw}(N)$ requires at most $N - 1$ pairwise comparisons to make a scheduling decision and hence has a computational complexity $O(N)^1$, since the complexity of each pairwise comparison based on $P_s^*(2)$ is $O(1)$ (due to the time-invariance property). In contrast, $CD^2$ based on solving the DP equations directly has a computational complexity of $O(n^N D)$ if $n_i = O(n)$ and $D_i = O(D) \forall i$.

V. SIMULATION RESULTS

In this section, we experimentally examine the performance of our proposed $CD^2$ scheduling policy. We compare $CD^2$ to the following benchmarks: Round Robin (RR), which schedules users in periodic fashion; Earliest Deadline First (EDF), which schedules the user with the most imminent deadline; and Best Channel First (BCF), which schedules the user with the best instantaneous channel condition. $CD^2$ jointly accounts for channel conditions, deadlines, and distortion costs in its scheduling decision. We consider two versions of each of the benchmark schedulers — a basic version which ignores packet distortion costs and transmits packets within a frame in sequential order, and a distortion-aware version which uses distortion information to reorder packets within a frame according to the prioritization rule described in Section II-B. Table II summarizes the decision criteria of all scheduling policies considered here.

We examine a system with four downlink users. Video frames for users arrive periodically to their respective queues at the BS, and get associated with a deadline equal to the period of arrival. A frame is comprised of multiple network packets. Any packets within a frame which are not successfully transmitted before deadline expiration are dropped, resulting in degradation of video quality at the corresponding downlink receiver. The received video quality is characterized by its PSNR (peak signal-to-noise ratio), defined as $\text{PSNR} \triangleq 10 \log_{10}(\frac{255^2}{\text{Distortion}})$. Distortion is measured in terms of mean-squared error. We use average PSNR (averaged over all four users) as a performance metric to compare different schedulers. PSNR is the most widely used metric for quantifying video quality. Typically, a 0.5dB difference in PSNR is noticeable, while a 2dB improvement in PSNR translates to significant improvement in perceived video quality.

In our simulation setup, each users wishes to receive 300 frames of the “Foreman sequence”

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1Let $m_N$ be the number of pairwise comparisons required by $\Pi_{pw}(N)$. Then, $m_N = N/2 + m_{N/2}$ if $N$ is even and $m_N = (N - 1)/2 + m_{(N+1)/2}$ if $N$ is odd. It is now easily verified that $m_N = (N - 1) \forall N$. 
(a commonly used test video sequence) at 352x288 pixels/frame (CIF format), 30 frames/sec, encoded using the new H.264/MPEG-4 AVC video compression standard [18] with a leading I-frame followed by 299 P-frames. All P-frames were chosen in order to produce a homogeneous stream of coded frames, in the sense that the coded frames (and associated packets) were a priori of approximately equal importance. The video was coded using H.264 reference software version JM10.2 [19]. Each coded frame was divided into independently decodable network packets of size 1500 bytes or less. This resulted in three to seven packets per frame, depending on the video content encoded in the frame. For example, a frame which captures a sudden scene change is likely to contain more packets than a frame which encodes a relatively static scene. “Frame copy error” concealment techniques were used to estimate missing information when one or more packets in a frame missed their decoding deadlines. A perfectly received copy of the Foreman sequence corresponds to a PSNR of 40.7dB. This establishes an upper-bound on the performance achievable by any scheduler. Note that this upper bound is finite because of the distortion introduced by lossy compression of the original video stream.

We used a two-state Gilbert-Elliot model for simulating bursty downlink wireless channels. The two states, GOOD and BAD, were associated with success probabilities $s_G$ and $s_B$ respectively, with $s_G > s_B$. The probability of transition (in every time-slot of duration $\sim 1.3$ms) from the GOOD to BAD state, as well as from the BAD to GOOD state, was fixed at 0.05. The success probabilities for users 2,3, and 4 were fixed at $s_B = 0.75$ and $s_G = 0.95, 0.97,$ and 0.99, respectively. Also, $s_G = 0.9$ was fixed for user 1, while $s_B$ was varied from 0.1 to 0.9, in steps of 0.1. For our choice of parameters, the stationary probability of being in either channel state is 0.5. Thus, the average success probability is computed as $s_{avg} = 0.5(s_G + s_B)$. Under the assumption of additive distortion across multiple packets [12], we simulated 100 channel realizations for each policy and for 9 different success probabilities, for a total of 7200 channel realizations. We contrasted the performance of CD$^2$ to other benchmark policies over identical channel realizations.

Fig. 4 depicts the average PSNR (averaged over all users) as a function of the average success probability for user 1 ($s_{avg}^1$), keeping $s_{avg}^2 = s_{avg}^3 = s_{avg}^4$ fixed. CD$^2$ comfortably outperforms the basic versions of RR, EDF, and BCF by several dB of PSNR. CD$^2$ also achieves significant
gains of 0.5-2dB over the distortion-aware versions of RR, EDF, and BCF. The improvement is largest over PSNR ranges where viewing is desired — 35dB. As the PSNR falls below 35dB, the perceived video quality falls quickly, and when it falls below roughly 30dB the quality can become unacceptable. Note that $CD^2$ achieves an average PSNR of 35dB at $s_{avg}^1 \approx 0.65$, whereas basic versions of benchmark schedulers do not achieve that performance level even at $s_{avg}^1 = 0.9$. There is a significant improvement in the performance of benchmark schedulers when they are allowed to prioritize packet transmissions based on per-packet distortion information. For instance, EDF with and without reordering drop an identical number of packets for each corresponding frame. However, EDF with reordering drops packets which cause the least amount of distortion, leading to 4-5dB gains. The results emphasize the importance of the preprocessing required to compute per-packet distortion information to include in packet headers to enhance system performance.

Fig. 5 shows the performance of the worst-case user for each policy. $CD^2$ achieves up to 4dB gains over the next best benchmark policy (distortion aware EDF). The gains are greater relative to average PSNR performance because the disparity between all users in the benchmark policies is quite large. However, for $CD^2$ the variance in PSNR across users is fairly small — the PSNR of the best user drops slightly in order to increase the PSNR of the worst user. Thus, $CD^2$ has better fairness properties than benchmark policies. $CD^2$ achieves a worst case PSNR of 35dB for $s_{avg}^1 \approx 0.73$, while none of the benchmarks (basic or distortion aware) achieve that mark even for $s_{avg}^1 = 0.9$. This clearly demonstrates the superiority of $CD^2$ under disparate channel conditions, a situation very likely to arise in real wireless systems where users far from the BS are more likely to experience poor channels.

Fig. 6 depicts the average number of packets dropped under each policy. Interestingly, in some cases $CD^2$ drops more packets than EDF and BCF, but the average PSNR for $CD^2$ is still significantly higher. This is attributed to the fact that EDF and BCF (both basic and distortion-aware versions) ignore channel conditions and frame deadlines respectively while making their scheduling decisions. In contrast, $CD^2$ jointly utilizes all available information to make more “intelligent” scheduling decisions.
VI. CONCLUSIONS

This paper examined the problem of scheduling multiple video streams across a shared wireless channel. We proposed the Channel, Deadline, and Distortion ($CD^2$) aware scheduling algorithm to provide a unified and systematic way to enhance system performance. $CD^2$ determines the best schedule based on channel characteristics, packet delay deadlines, and packet importance, and prioritizes transmission of packets within a stream as well as across multiple streams, in order to minimize the expected aggregate distortion across all of the video streams. Our experimental results show that $CD^2$ provides significant gains vis-à-vis benchmark schedulers.

REFERENCES

A. Proof of Lemma 1

Denote $\beta(x, y, s) \triangleq \binom{x}{y} s^y (1-s)^{x-y}$. Two distinct cases arise:

1) $y \geq t$: At least $y - t$ packets get dropped. Additionally, $t - j$ packets get dropped w.p. $\beta(t, j, s_2)$. Thus, a total of $y - j$ packets get dropped w.p. $\beta(t, j, s_2)$, implying $\phi_2(y, t) = \sum_{j=0}^{y} \omega_2(y-j)\beta(t, j, s_2)$.

2) $y \leq t$: Consider each channel use as equivalent to a coin toss with bias $s_2$. If $y$ or more tosses result in success, no packets are dropped. If $j < y$ tosses result in success, $y - j$ packets get dropped. Thus, $\phi_2(y, t) = \sum_{j=0}^{y} \omega_2(y-j)\beta(t, j, s_2)$.

Combining the two cases, we get the desired result.

B. Proof of Lemma 2

For $y \geq t$, $\phi_2(y, t) = \mathbb{E}_J[\omega_2(y - J)]$, which is a non-negative linear combination of non-increasing and convex functions, and hence inherits the same properties. For $y < t$, we have

$$\phi_2(y + 1, t) - \phi(y, t) = \sum_{j=0}^{y} \omega_2(y-j+1) - \omega_2(y-j) \beta(t, j, s_2) \geq 0, \quad (9)$$

$$\phi_2(y + 1, t) - 2\phi_2(y, t) + \phi_2(y - 1, t) = \sum_{j=0}^{y-1} [\omega_2(y-j+1) - 2\omega_2(y-j) + \omega_2(y-j-1)] \beta(t, j, s_2) + \omega_2(1) \beta(t, y, s_2) \geq 0, \quad (10)$$

implying the desired result.
C. Proof of Lemma 3

The proof is based on inductive arguments.

1) Base Case \( t = T \): From (4), (6), and the boundary conditions for the two-user problem it follows that \( \gamma^T(n) = -s_1[\omega_1(n_1) - \omega_1(n_1 - 1)] + s_2[\phi_2(n_2) - \phi_2(n_2 - 1)] \). Since \( \omega_1(\cdot) \) is convex (by assumption) and \( \phi_2(\cdot) \) is convex (by Lemma 2), the desired result follows.

2) Inductive Step \( t < T \): We will show that \( \gamma^t(n) \) is a non-decreasing function of \( n_1 \). The proof for monotonicity of \( \gamma^t(n) \) as a function of \( n_2 \) is similar. We assume that the hypothesis of the lemma is true in all states \( n \) in time-slot \( t + 1 \), for some \( t < T \). We introduce the following notation for the sake of compactness: \( \Delta_t f^t(n) \triangleq f^t(n) - f^t(n - e_i) \) and \( \Delta^t_{ij}(n) \triangleq \Delta_t f^t(n) - \Delta_t f^t(n - e_j) \) for \( i, j = 1, 2 \) and any function \( f^t(n) \). Now, by definition

\[
\begin{align*}
\gamma^t(n) & = -s_1 \Delta_1 V^{t+1}(n) + s_2 \Delta_2 V^{t+1}(n) \\
\gamma^t(n + e_1) & = -s_1 \Delta_1 V^{t+1}(n + e_1) + s_2 \Delta_2 V^{t+1}(n + e_1) \\
\gamma^t(n + e_2) & = -s_1 \Delta_1 V^{t+1}(n + e_2) + s_2 \Delta_2 V^{t+1}(n + e_2)
\end{align*}
\]

We want to show that \( \Delta_1 \gamma^t(n + e_1) \leq 0 \). From (11),

\[
\begin{align*}
\Delta_1 \gamma^t(n + e_1) & = -s_1 \Delta_{11} V^{t+1}(n + e_1) + s_2 \Delta_{12} V^{t+1}(n + e_1) \\
\Delta_2 \gamma^t(n + e_2) & = -s_1 \Delta_{21} V^{t+1}(n + e_2) + s_2 \Delta_{22} V^{t+1}(n + e_2)
\end{align*}
\]

Five different cases arise, depending on whether \( \mathcal{P}_2^*(2) \) schedules \( Q_1 \) or \( Q_2 \) in states \( n - e_1, n, n - e_2, n + e_1, \) and \( n + e_1 - e_2 \) in time-slot \( t + 1 \). Due to space constraints, we present details only for two representative cases. The remaining three cases can be treated in similar fashion.

- **Case 1:** \( \mathcal{P}_2^*(2) \) schedules \( Q_1 \) in states \( n - e_1, n, n - e_2, n + e_1, \) and \( n + e_1 - e_2 \) in time-slot \( t + 1 \). In this case, we have the following sets of equalities:

\[
\begin{align*}
\Delta_1 V^{t+1}(n + e_1) & = s_1 \Delta_{11} V^{t+2}(n) + s_1 \Delta_{11} V^{t+2}(n + e_1) \\
\Delta_1 V^{t+1}(n + e_1) & = s_1 \Delta_{12} V^{t+2}(n) + s_1 \Delta_{12} V^{t+2}(n + e_1) \\
\Delta_1 \gamma^{t+1}(n) & = -s_1 \Delta_{11} V^{t+2}(n) + s_2 \Delta_{12} V^{t+2}(n) \\
\Delta_1 \gamma^{t+1}(n + e_1) & = -s_1 \Delta_{11} V^{t+2}(n + e_1) + s_2 \Delta_{12} V^{t+2}(n + e_1).
\end{align*}
\]
Combining the above with (12) we get,

\[\Delta_1 \gamma_t^t(n + e_1) = s_2 \Delta_1 \gamma^{t+1}(n + e_1) + s_2 \Delta_1 \gamma^{t+1}(n + e_1) \leq 0,\]  

where the non-negativity of the terms on the right follows from our inductive assumption.

- **Case 2:** \(P_2^*(2)\) schedules \(Q_2\) in states \(n - e_1, n, n - e_2, n + e_1\) and \(n + e_1 - e_2\) in time-slot \(t + 1\). In this case, we have the following set of equalities:

\[
\begin{align*}
\Delta_1 V^{t+1}(n + e_1) - \Delta_1 V^{t+1}(n) &= s_2 \Delta_1 V^{t+2}(n + e_1) + s_2 \Delta_1 V^{t+2}(n + e_1) \\
\Delta_2 \gamma^{t+1}(n + e_1) &= -s_1 \Delta_2 V^{t+2}(n + e_1) + s_2 \Delta_2 V^{t+2}(n + e_1) \\
\Delta_2 \gamma^{t+1}(n + e_1 - e_2) &= -s_1 \Delta_2 V^{t+2}(n + e_1 - e_2) + s_2 \Delta_2 V^{t+2}(n + e_1 - e_2).
\end{align*}
\]

Combining the above with (12) we get,

\[\Delta_1 \gamma_t^t(n + e_1) = s_2 \Delta_1 \gamma^{t+1}(n + e_1 - e_2) + s_2 \Delta_1 \gamma^{t+1}(n + e_1) \leq 0.\]  

The hypothesis of the lemma now follows from the principle of mathematical induction.

**D. Proof of Theorem 1**

Recall that \(P_2^*(2)\) is fully characterized by the sign of \(\gamma^t\). For fixed \(t\), it follows from Lemma 3 that \(\gamma^t\) changes sign at most once from negative to positive as \(n_2\) increases for fixed \(n_1\). Thus, for fixed \(n_1\), \(\exists n_2 = \psi^t(n_1)\) such that the optimal decision switches over from \(Q_1\) to \(Q_2\) in state \((n_1, \psi^t(n_1))\). Since \(\gamma^t\) is a non-increasing function of \(n_1\), it follows that \(\gamma^t(n_1', n_2)\) can change sign only later than \(\gamma^t(n_1, n_2)\) for fixed \(n_1' > n_1\) as \(n_2\) increases, implying \(\psi^t(n_1') > \psi^t(n_1)\). The desired result follows from the definition of a switch-over policy.

**E. Proof of Theorem 2**

We will show that \(\text{sgn}[\gamma^{t+1}(n)] = \text{sgn}[\gamma^t(n)] \ \forall \ t < T, \ \forall \ n\), where \(\text{sgn}[x] = 1\) if \(x \geq 0\) and \(\text{sgn}[x] = -1\) if \(x < 0\). Since the optimal decision in time-slot \(t\) is completely determined by the
sign of $\gamma^t$, the implication is that the decisions of $\mathcal{P}_s^*(2)$ are identical in time-slot $t$ and time-slot $t+1$ for every state. Since $t$ is arbitrarily chosen, the claim of the theorem follows.

We first assume that $\gamma^{t+1}(n) \leq 0$. Lemma 3 implies that $\gamma^{t+1}(n - e_2) \leq 0$. However, $\gamma^{t+1}(n - e_1)$ could be negative or positive. Accordingly, we have two cases:

- $\gamma^{t+1}(n - e_1) \leq 0$: In this case,

$$V^{t+1}(n) = s_1 V^{t+2}(n - e_1) + s_1 V^{t+2}(n)$$

$$V^{t+1}(n - e_2) = s_1 V^{t+2}(n - e_1 - e_2) + s_1 V^{t+2}(n - e_2)$$

$$V^{t+1}(n - e_1) = s_1 V^{t+2}(n - 2e_1) + s_1 V^{t+2}(n - e_1). \quad (15)$$

From (15), $\gamma^t(n) = s_1 \gamma^{t+1}(n - e_1) + s_1 \gamma^{t+1}(n) \leq 0$.

- $\gamma^{t+1}(n - e_1) > 0$: In this case,

$$V^{t+1}(n) = s_1 V^{t+2}(n - e_1) + s_1 V^{t+2}(n)$$

$$V^{t+1}(n - e_2) = s_1 V^{t+2}(n - e_1 - e_2) + s_1 V^{t+2}(n - e_2)$$

$$V^{t+1}(n - e_1) = s_2 V^{t+2}(n - e_1 - e_2) + s_1 V^{t+2}(n - e_1). \quad (16)$$

From (16), $\gamma^t(n) = s_1 \gamma^{t+1}(n) \leq 0$.

Using Lemma 3 and the definition of $\gamma^t(n)$, we can establish analogous results under the assumption $\gamma^{t+1}(n) > 0$. In conclusion, $\text{sgn}[\gamma^t(n)] = \text{sgn}[\gamma^{t+1}(n)]$.

**F. Proof of Theorem 3**

For ease of exposition, we outline the proof for the case $N = 3$. The proof presented here extends in a natural way to $N > 3$. By definition,

$$\gamma_{12}^t(n) = s_1 V^{t+1}(n - e_1) - s_2 V^{t+1}(n - e_2) + (s_2 - s_1)V^{t+1}(n). \quad (17)$$

We want to show that $\text{sgn}[\gamma_{12}^t(n)] = \text{sgn}[\gamma_{12}^t(n^{12})]$ for $t = 1, \ldots, T$, where $n = (n_1, n_2, n_3)$ with $n_3 > 0$ and $n^{12} = (n_1, n_2, 0)$. In words, the result of the comparison between $Q_1$ and $Q_2$ is unaffected by the presence of $Q_3$. The proof is based on inductive arguments.
1) Base Case \((t = T)\): From (17) and the boundary conditions, 
\[ \gamma_{12}^T(n) = s_1[\omega_1(n_1) - \omega_1(n_1 - 1, 1)] + s_2[\omega_2(n_2) - \omega_2(n_2 - 1)], \]  
which is independent of \(n_3\), thereby completing the proof.

2) Inductive Step \((t < T)\): We assume that the hypothesis of the theorem is true in time-slot \(t + 1\). Several cases arise, depending on the decision of \(P_s^*(3)\) in states \(n - e_1, n - e_2\) and \(n\) in time-slot \(t + 1\). Due to space constraints, we only treat three representative cases. All other cases can be treated in similar fashion.

- \(P_s^*(3)\) schedules \(Q_1\) in states \(n - e_1, n - e_2\) and \(n\) in time-slot \(t + 1\): In this case, we can show 
\[ \gamma_{12}^t(n) = s_1\gamma_{12}^{t+1}(n - e_1) + (1 - s_1)\gamma_{12}^{t+1}(n) \leq 0, \]  
where the inequality follows because \(\gamma_{12}^{t+1}(n - e_1) \leq 0\) and \(\gamma_{12}^{t+1}(n) \leq 0\) by assumption. Also, our inductive assumption implies that \(\Pi_{PW}(N)\) schedules \(Q_1\) in states \(n^{12} - e_1\) and \(n^{12}\) in time-slot \(t + 1\), implying 
\[ \gamma_{12}^{t+1}(n^{12} - e_1) \leq 0 \]  
and 
\[ \gamma_{12}^{t+1}(n^{12}) \leq 0. \]  
It follows, 
\[ \gamma_{12}^{t}(n^{12}) = s_1\gamma_{12}^{t+1}(n^{12} - e_1) + (1 - s_1)\gamma_{12}^{t+1}(n^{12}) \leq 0. \]  
We conclude \(\text{sgn}[\gamma_{12}^t(n)] = \text{sgn}[\gamma_{12}^t(n^{12})] = -1\), as desired.

- \(P_s^*(3)\) schedules \(Q_2\) in states \(n - e_1, n - e_2\) and \(n\) in time-slot \(t + 1\): In this case, we can show 
\[ \gamma_{12}^t(n) = s_2\gamma_{12}^{t+1}(n - e_2) + (1 - s_2)\gamma_{12}^{t+1}(n) > 0, \]  
where the inequality follows from our assumption. Also, our inductive assumption implies that \(\Pi_{PW}(N)\) schedules \(Q_2\) in states \(n^{12} - e_2\) and \(n\) in time-slot \(t + 1\), implying 
\[ \gamma_{12}^{t+1}(n^{12} - e_2) \leq 0 \]  
and 
\[ \gamma_{12}^{t+1}(n^{12}) \leq 0. \]  
It follows, 
\[ \gamma_{12}^{t}(n^{12}) = s_2\gamma_{12}^{t+1}(n^{12} - e_2) + (1 - s_2)\gamma_{12}^{t+1}(n^{12}) \leq 0. \]  
We conclude \(\text{sgn}[\gamma_{12}^t(n)] = \text{sgn}[\gamma_{12}^t(n^{12})] = +1\), as desired.

- \(P_s^*(3)\) schedules \(Q_2\) in states \(n - e_1, n - e_2\) and \(n\) in time-slot \(t + 1\): In this case, we can show 
\[ \gamma_{12}^t(n) = s_3\gamma_{12}^{t+1}(n - e_3) + (1 - s_3)\gamma_{12}^{t+1}(n) \leq 0, \]  
Now, our inductive assumption implies that 
\[ \text{sgn}[\gamma_{12}^{t+1}(n - e_3)] = \text{sgn}[\gamma_{12}^{t+1}(n)] = \text{sgn}[\gamma_{12}^{t+1}(n^{12})]. \]  
Thus, we conclude 
\[ \text{sgn}[\gamma_{12}^t(n)] = \text{sgn}[\gamma_{12}^t(n^{12})] = \text{sgn}[\gamma_{12}^t(n^{12})], \]  
where the last equality follows from Theorem 2.

We have established that \(\text{sgn}[\gamma_{12}^t(n)] = \text{sgn}[\gamma_{12}^t(n^{12})].\) Using similar analysis, we can establish synonymous equalities for \(\gamma_{23}^t\) and \(\gamma_{31}^t\), and also extend the results to \(N > 3\).
Repeat:
• If $Q^t = \emptyset\dagger$, quit.
• If $Q^t = \{k\}$, schedule $Q_k$ and quit.
• Set $U = \emptyset$ and $Q = Q^t$. Repeat:
  – If $Q = \emptyset$, quit.
  – If $Q = \{k\}$, set $U = U \cup \{k\}$, $Q = \emptyset$.
  – If $|Q| \geq 2$, select $k \neq l$ randomly from $Q$.
  – Use $P_s^t(2)$ to choose one of either $Q_k$ or $Q_l$.
  – If $Q_k$ is chosen, set $U = U \cup \{k\}$, else set $U = U \cup \{l\}$. In both cases, set $Q = Q \setminus \{k, l\}$.
• Set $Q^t = U$.
\dagger $Q^t$ denotes the set of scheduling candidates (non-empty queues) in time-slot $t$.

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TABLE II
DECISION CRITERIA FOR DIFFERENT SCHEDULING POLICIES

Fig. 1. Schematic of the wireless downlink with $N$ parallel queues and a single time-multiplexed scheduler $S$ at the base-station.
Fig. 2. Plots of $\omega_i(k_i)$ for four different frames of the Foreman sequence.

Fig. 3. A typical switch-over curve; $\circ$ and $\bullet$ denote the states in which it is optimal to schedule $Q_1$ and $Q_2$, respectively.
Fig. 4. Performance gains for 4 user case: Average PSNR (in dB) versus average probability of successful transmission for user 1, $s_{avg}^1$.

Fig. 5. Performance gains for 4 user case: Worse Case PSNR (in dB) versus average probability of successful transmission for user 1, $s_{avg}^{1^{worse}}$. 
Fig. 6. Packet drop rate versus average probability of successful transmission for user 1, $s_1^{avg}$.